

MS JUNIOR COLLEGE
Hyderabad

GUESS PAPER - 2
INTERMEDIATE 2nd YEAR
MATHEMATICS- IIA

Time: 3hours

Max.Marks:75

- I. i) Very Short Answer Type Questions. (10 x 2 = 20)
ii) Answer **ALL** questions.
iii) Each question carriers **TWO** marks.
1. Find the Squares root of $7 + 24i$.
 2. Express $-1 - \sqrt{3}i$ in modulus - amplitude form.
 3. If the cube roots of unity are $1, \omega, \omega^2$, then find the roots of the equation $(x - 1)^3 + 8 = 0$.
 4. Find the quadratic equation, the sum of whose roots is 7 and the sum of the squares of the roots is 25.
 5. If the product of roots of $4x^3 + 16x^2 - 9x - a = 0$ is 9 then find a.
 6. Find the number of palindromes with 6 digits that can be formed using the digits 1, 3, 5, 7, 9.
 7. Find the number of positive divisors of 1080.
 8. If the coefficients of $(2r + 4)^{\text{th}}$ term and $(3r + 4)^{\text{th}}$ term in the expansion of $(1 + x)^{21}$ are equal, then find r.
 9. Find the variance of the data 5, 12, 3, 18, 6, 8, 2, 10.
 10. The range of a random variable X is $\{1, 2, 3, \dots, \infty\}$ and $P(X = k) = \frac{c^k}{k!}$; $k = 1, 2, 3, \dots, \infty$, find c.
- II. i) Short Answer Type Questions. (5 x 4 = 20)
ii) Answer any **FIVE** questions.
iii) Each question carriers **FOUR** marks.
11. If the amplitude of $\left(\frac{z-2}{z-6i}\right) = \frac{\pi}{2}$, find its locus.
 12. Solve the equation $\sqrt{\frac{3x}{x+1}} + \sqrt{\frac{x+1}{3x}} = 2$.
 13. Find the number of ways of arranging 5 different mathematics books, 4 different physics books and 3 different chemistry books such that the books of the same subject are together.
 14. Show that $\frac{{}^{4n}C_{2n}}{{}^{2n}C_n} = \frac{1.3.5\dots(4n-1)}{\{1.3\dots(2n-1)\}^2}$.
 15. Resolve into partial fractions $\frac{x^4}{(x-1)(x-2)}$.
 16. A speaks truth in 75% of the cases and B in 80% of the cases. What is the probability that their statements about an incident do not match.
 17. A, B are two independent events such that the probability of both the events to occur is 1/6 and the probability of both the events do not occur is 1/3. Find P(A).

III. i) Long Answer Type Questions.

(5 x 7 = 35)

ii) Answer any **FIVE** questions.

iii) Each question carries **SEVEN** marks.

18. Find all the roots of the equation $x^9 - x^5 + x^4 - 1 = 0$.

19. Solve the equation $x^4 + 4x^3 - 2x^2 - 12x + 9 = 0$, if it has a pair of equal roots.

20. Prove that $C_0 C_r + C_1 C_{r+1} + C_2 C_{r+2} + \dots + C_{n-r} C_n = {}^{2n}C_{n+r}$.

Deduce that i) $C_0^2 + C_1^2 + C_2^2 + \dots + C_n^2 = {}^{2n}C_n$. ii) $C_0 C_1 + C_1 C_2 + C_2 C_3 + \dots + C_{n-1} C_n = {}^{2n}C_{n+1}$.

21. If $|x|$ is so small that x^2 and higher powers of x may be neglected, then find approximate value of

$$\frac{\left(1 - \frac{2x}{3}\right)^{\frac{3}{2}} (32 + 5x)^{\frac{1}{5}}}{(3-x)^3}$$

22. Find the mean deviation from the median of the following data.

Age (Years)	20-25	25-30	30-35	35-40	40-45	45-50	50-55	55-60
No. of workers (f_i)	120	125	175	160	150	140	100	30

23. Three boxes numbered I, II, III contain 1 white, 2 black and 3 red balls; 2 white, 1 black and 1 red ball; 4 white, 5 black and 3 red balls respectively. One box is randomly selected and a ball is drawn from it. If the ball is red then find the probability that it is from box II.

24. The range of a random variable X is $\{0, 1, 2\}$. Given that $P(X=0) = 3C^3$, $P(X=1) = 4C - 10C^2$, $P(X=2) = 5C - 1$. Find (i) the value of C (ii) $P(X < 1)$ (iii) $P(1 < X \leq 2)$ (iv) $P(0 < X \leq 3)$.
